

Teaching Pack

Mensuration – The circle

Cambridge IGCSETM

Mathematics 0580

This *Teaching Pack* can also be used with the following syllabuses:

• Cambridge IGCSE™ (9–1) Mathematics **0980**

• Cambridge IGCSE™ International Mathematics **0607**

• Cambridge O Level Mathematics **4024**



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| **Icons used in this pack:** | |
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Introduction

This *Teaching Materials* *Pack* focuses on supporting learners to develop confidence and fluency with the formulas associate with the circumference and area of a circle. Also derive and use the formulas for the arc length and area of a sector.

The lessons presented here are designed for learners that are already familiar with the concept of a circle and the parts of a circle so they can apply this understanding to the circumference, arc length and sectors of circles.

It is expected that learners should already understand the concept of perimeter as a distance around a shape and area as the amount of space inside the boundary of a flat (2-dimensional) object such as a circle. They should also understand the concept of units in terms of measurements of distance and area (unit squared).

It would be useful if students could also multiply a whole number by a fraction both using a calculator and using written methods. It would also be useful if they could simplify fractions.

**Important note**

Our *Teaching Packs* have been written by **classroom teachers** to help you deliver topics and skills that can be challenging. Use these materials to supplement your teaching and engage your learners. You can also use them to help you create lesson plans for other skills.

***This content is designed to give you and your learners the chance to explore mathematical skills. It is not intended as specific practice for exam papers.***

This is one of a range of Teaching Packs. Each pack is based on one mathematical topic with a focus on specific mathematical techniques. The packs can be used in any order to suit your teaching sequence.

In this pack you will find the lesson plans and worksheets you will need to successfully complete the teaching of this topic.

Skill: Mensuration – The circle

This *Teaching Pack* links to the following syllabus content (see syllabus for detail):

* C5.2 Carry out calculations involving the circumference and area of a circle

Solve simple problems involving the arc length and sector area as fractions of the circumference and area of a circle.

* E5.2 Carry out calculations involving the circumference and area of a circle.

Solve problem involving the arc length and sector area as fractions of the circumference and area of a circle.

|  |
| --- |
| For assessments from 2025 |
| * C5.3 Carry out calculations involving the circumference and area of a circle.  Carry out calculations involving arc length and sector area as fractions of the circumference and area of a circle, where the sector angle is a factor of 360°. * E5.3 Carry out calculations involving the circumference and area of a circle.  Carry out calculations involving arc length and sector area as fractions of the circumference and area of a circle. |

****The pack covers mathematical skills, adapted from **AO1: Demonstrate knowledge and understanding of mathematical techniques / Knowledge and understanding of mathematical techniques** and **AO2: Reason, interpret and communicate mathematically when solving problems / Analyse, interpret and communicate mathematically**.

**Before you begin**

This *Teaching Pack* includes a **Teacher Introduction** video to which you should refer before   
using the resources in this pack. The video is available to watch in Resource Plus within the topic section relevant to this **Teaching Pack**.

The video introduces the resources available for teaching this topic, and explains how they can be used to successfully deliver the topic to your learners. In particular, the video highlights typical learner misconceptions and common errors this *Teaching Pack* will help you to overcome.

****Lesson 1 – Circumference of a circle

|  |  |
| --- | --- |
| **Resources** | * Lesson 1 presentation * Activity 1 * Worksheet 1 |
| **Learning objectives** | By the end of the lesson learners should be able to:   * carry out calculations involving the circumference of a circle. |

| **Timings** | | **Activity** |
| --- | --- | --- |
|  | **Starter / Introduction**  **Slide 2 – 3** Use this activity to check learners’ knowledge of the different parts of the circle. This activity can also be done in groups as a reading images activity by printing the slide without the boxes/answers and asking learners to reproduce the diagram. Using this approach, learners work in small groups and one person at a time comes up and looks at the image for a short period (approximately 30 seconds). They then go back to the group and try to explain to the group how to reproduce the image. They cannot touch or draw on the image themselves. It might be useful to provide a blank circle template for learners to use if approaching this activity in this way.  Explain to learners what is meant by a minor arc or segment. Tell them we will be looking at arcs and sectors later in this series of lessons but for the first two lessons we will be focusing on the perimeter and the area of a circle. | |
|  | **Main lesson**  **Slide 4** This fill in the gap activity is designed to test learners understanding of pi number. Complete this as a whole class activity, clicking to show the answers.  **Slide 5 –** [Activity 1](#act1) - you can use this activity to investigate the formulae for the circumference of a circle or you can go straight to presenting the formula using **slides 6**.  Work through the examples **Slides 7 to 9.** Tell learners it is generally useful to draw a diagram. Pause to give learners the opportunity to work out the answers independently before moving on to answers. The example on **slide 8** introduces the use of as an approximation for π. | |
|  | **Plenary**  Summarise the learning in the lesson and introduce:  **Homework –** [Worksheet 1](#wk1) | |

****Lesson 2 – Area of a circle

|  |  |
| --- | --- |
| **Resources** | * Lesson 2 presentation * Scissors * Worksheet 2 Area of a circle |
| **Learning objectives** | By the end of the lesson learners should be able to:   * carry out calculations involving the area of a circle. |

| **Timings** | | **Activity** |
| --- | --- | --- |
|  | **Slides 2 - 6 Area of a circle** This practical activity gives learners the opportunity to see how the formula for the area of a circle can be approximated. | |
|  | **Slide 7** demonstrates how the formula can be rearranged depending on the information that you are given in the question. Give learners the opportunity to do the rearrangements before animating the slides by clicking on the boxes. The final rearrangement may need some further explanation depending on the group you are working with.  **Slide 8 to 11** work through a series of examples that demonstrate how to use the different rearrangements depending on the information in the question. | |
|  | **Plenary**  What is the minimum information you need to be able to find the circumference and area of a circle? *The minimum information you need is either the length of the radius or the diameter.*  How would you go about finding the area of a circle if you know the circumference? *The formula for area of a circle is πr2. The formula for the circumference is 2πr*. *You can rearrange this second formula to make r the subject r = . You can then substitute this into the formula for the area. Area =  = .*  Why is it easy to distinguish between the formulae for the circumference and area of a circle? *The formula for the circumference is 2πr or πd. In either case it only uses r once, so it is a measure of length. The formula for area of a circle is πr2. In this case the length (the radius) is squared so this is a measure of area.*  All circles are similar. Use what you know about the ratio of the circumference to the diameter of a circle to help you explain this. *The ratio of the circumference to the diameter for all circles will always approximate to π. Therefore, all circles are similar.*  **Homework** – [Worksheet 2](#wk2) | |

****Lesson 3 – Arc length and sector areas

|  |  |
| --- | --- |
| **Resources** | * Lesson 3 presentation * Worksheet 3 * Activity 2 Constructing Polygons |
| **Learning objectives** | By the end of the lesson should be able to:   * solve simple problems involving the arc length and sector area as fractions of the circumference and area of a circle |

| **Timings** | | **Activity** |
| --- | --- | --- |
|  | **Slide 2** Remind learners what the sector, arc and radius of a circle are. | |
|  | **Slide 3** Use exampleto explain how you calculate the fraction of the circle enclosed in a sector when you know the angle at the centre of that sector.  **Slides 4** Use to show how you can calculate the length of the arc once you know the fraction of the whole circle enclosed in the arc.  **Slide 5** extends this work to demonstrate how you work out the area of the sector again using a specific example.  **Slide 6** presents the general formula. Give learners the opportunity to fill in the boxes before you animate the slide.  **Slide 7 and 8** Work through a series of examples that demonstrate how to calculate arc length and area of a sector.  [Activity 2 Constructing Polygons](#act2) **(Extension activity)** This activity will also prepare students for the first activity in the circle theorem series lessons. | |
| Chart, icon  Description automatically generated | **Plenary**  Summarise the learning in the lesson and introduce:  **Homework –** [Worksheet 3](#wk3) | |

Teacher’s notes

Key words / concepts you could highlight during the lesson, or have pre-taught before the lesson:

Students need a basic understanding of perimeter before tackling lesson 1.

**Key words**

* Perimeter
* Circumference
* Area
* Radius
* Diameter
* Arc
* Sector
* Chord

The time required for Lesson 1 will depend on whether the activity is used and how quickly the students become competent and fluent with the formula for the circumference. Depending on these two points you may want to combine lessons1 and 2 as a single lesson.

**** Worksheets and answers

|  |  |  |
| --- | --- | --- |
|  | **Worksheets** | **Answers** |
| **For use in *Lesson 1:*** |  |  |
| **Activity 1:** Circumference investigation | **12** |  |
| **Worksheet 1:** Circumference of a circle | **15** | **17** |
|  |  |  |
| **For use in *Lesson 2:*** |  |  |
| **Worksheet 2:** Area of a circle | **18** | **20** |
|  |  |  |
| **For use in *Lesson 3:*** |  |  |
| **Worksheet 3:** Arc length and sector area | **22** | **24** |
| **Activity 2:** Constructing a Polygon | **25** | **26** |

Activity 1

Task

1. Work out the diameters for each of the circles on the next two pages.

2. Using a piece of string measure the circumferences of each circle.

1. Fill in the table

4. Complete the table by calculating for each circle

|  |  |  |  |
| --- | --- | --- | --- |
| **Radius**  **r (cm)** | **Diameter**  **d (cm)** | **Circumference**  **C (cm)** |  |
| 2 |  |  |  |
| 3 |  |  |  |
| 4 |  |  |  |
| 5 |  |  |  |
| 6 |  |  |  |

**Conclusion**

=

C =

Activity 1 – continued

2 cm

3 cm

4 cm

Activity 1 – continued

5 cm

6 cm

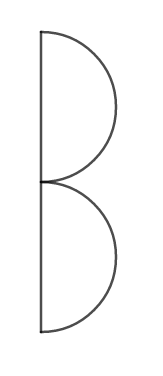
Worksheet 1

Use this sheet to become confident and fluent with using the formula for the circumference of a circle to answer a range of problems.

1. Fill in the gaps

* A circle is a set of points that are at a given distance from its…………………….
* The…………………………………….. is the distance round the circle
* The………………….. is the distance from the centre to the………………………………

1. A circular pool has radius 8 m. Calculate the circumference of the pool.
2. A circle has a radius of 6.4 cm. Work out the circumference of the circle.



15cm

15cm

1. A letter B is made out of a piece of wire.   
   It has a straight side and to equal semicircles.   
   How much wire is required to make this letter?

Worksheet 1 – continued

**Extension questions**

1. Abjit’s bicycle wheel has a radius of 29 cm.
   1. Calculate the circumference of the wheel. Give your answer correct to 1 decimal place.
   2. Calculate the number of complete turns the wheel makes when travelling 500 m.
2. All curves in the left-hand figure semicircles. All curves in the right-hand figure are quarter circles or three-quarter circles. Calculate the perimeter of each shape.

A close up of a lamp

Description automatically generatedA picture containing object, lamp, sitting

Description automatically generated

2cm

2cm

2cm

4cm

Worksheet 1 – Answers

1. Fill in the gaps

* A circle is a set of points that are at a given distance from its centre.
* The circumference is the distance round the circle
* The radius is the distance from the centre to the circumference.

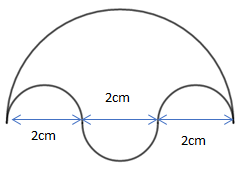
1. Circumference of one semicircle =

Circumference of letter B =

77.1 cm wire is required to make this letter.

1. (a) (b)

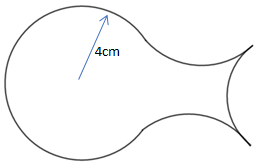
The wheel will make 274 complete turns.



1. Circumference of the big semicircle

Circumference of one small semicircle

Circumference of the shape = 9.42 + 3 x 3.14 = 18.84 cm

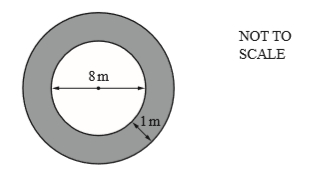


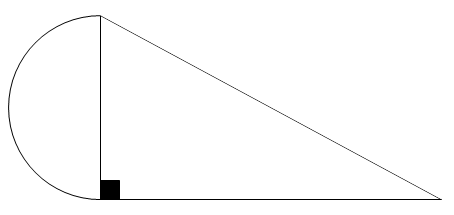
Circumference of big circle

Circumference of small circle

Circumference of the shape =

Worksheet 2

1. Work out the shaded area in this diagram. Give your answer in terms of π.

1. The diagram shows a shape made from a semicircle, radius 8 cm and a right-angled triangle with the hypotenuse of 25 cm.
   1. Find x.
   2. Calculate the area of the shape.

Give your answers correct to one decimal place.

X cm

* 1. A small Pizza has a diameter of 25 cm. What is the surface area of the top of the pizza?
  2. A large pizza has twice the surface area of the small one. What is the diameter of the large pizza?

Give your answers correct to 2 decimal places.

1. A door is in the shape of a rectangle with a semi-circular arch on top. The rectangular part is 2m high and the door is 90cm wide. What is the area of the door? Give your answers correct to 2 decimal places.

Worksheet 2 – continued

**Extension questions**

1. A solid cylinder has length 15 cm and radius 6 cm.A picture containing sport

   Description automatically generated

Calculate the total surface area of the cylinder. Give your

answer in terms of π.

1. Running track. The inside perimeter of a running track has the shape below. Both straights are 80m. Both ends are identical semicircles. The track is 8 m wide. What is the area of the

smallest rectangular field needed to contain it?  
  
A picture containing athletic game, sport

Description automatically generated

1. The diagram below shows a solid circular cone and a solid sphere.

A close up of a piece of paper

Description automatically generated

The cone has radius 5x cm and height 12x cm.

The sphere has radius r cm.

The cone has the same **total** surface area as the sphere.

Show that

[The curved surface area, *A*, of a cone with radius r and slant height l is *A* =πrl.]

[The surface area, *A*, of a sphere with radius r is *A* = 4πr2.]

Worksheet 2 – Answers

1. Area of the large circle =

Area of the small circle =

Area of the shaded area = Area of the large circle – area of the small circle

Area of the shaded area =

1. (a)

(b)

Area of the triangle =

Area of the semicircle =

Area of the shape =

1. (a)

Area of the small pizza =

(b)

Area of the large pizza =

Radius of the large pizza =

Diameter of the large pizza =

1. Area of the rectangle =

Area of the semicircle =

Worksheet 2 – Answers

**Extension questions**

1. Area of the cylinder

Area of the cylinder =

1. Area of the smallest field is =
2. Slant height =

Worksheet 3

1. *OAB* is a sector of a circle with radius 9 cm and centre *O*. Calculate the area of this sector. Give your answers in terms of π.

A close up of text on a white background

Description automatically generated

1. A close up of a map

   Description automatically generatedThe diagram shows a sector of a circle, centre *O*, radius 25 cm. Calculate the length of the arc AB. Give your answer correct to 4 significant figures.
2. The perimeter of this sector of a circle is 28.2 cm.

Calculate the value of c.

A screenshot of a cell phone

Description automatically generated

Worksheet 3 - continued

A close up of a map

Description automatically generated

1. AB is an arc of a circle, centre *O*, radius 9 cm.

The length of the arc *AB* is 6π cm.

The area of sector *AOB* is kπ cm2.

Find the value of k.

Worksheet 3 – Answers

2. Arc length =
3. Perimeter of the sector =
4. Length of *AB* =

Angle *AOB* = 120o

Area of Sector *AOB* =

Activity 2

A close up of a person

Description automatically generatedLook at this diagram. It is constructed by using two radii together with a chord of the circle which links the points were two radii touch the circumference of the circle.

What type of triangle is formed how can you justify this?

A picture containing object

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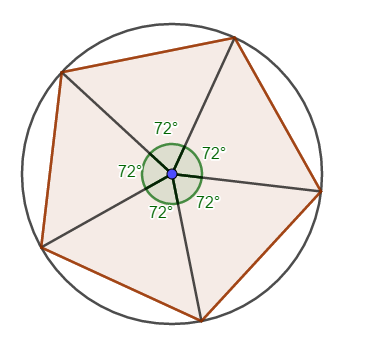
Use this diagram to demonstrate how if you continue to form equal sectors around the circle this can help you to draw a regular polygon. The resulting polygon is called an inscribed polygon because it is drawn inside the circle.

Explain why if you draw a chord the same length as the radius of the circle the inscribed polygon you will get will be a hexagon.

Activity 2–Constructing Polygons Exemplar Solution

A picture containing object

Description automatically generated



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